

On the Relationship Between Probabilistic Circuits and Determinantal Point Processes

Honghua Zhang, Steven Holtzen and Guy Van den Broeck

Computer Science Department, University of California, Los Angeles

{hzhang19, sholtzen, guyvdb}@cs.ucla.edu

PCs and DPPs

Probabilistic
Circuits

Positive
Dependence

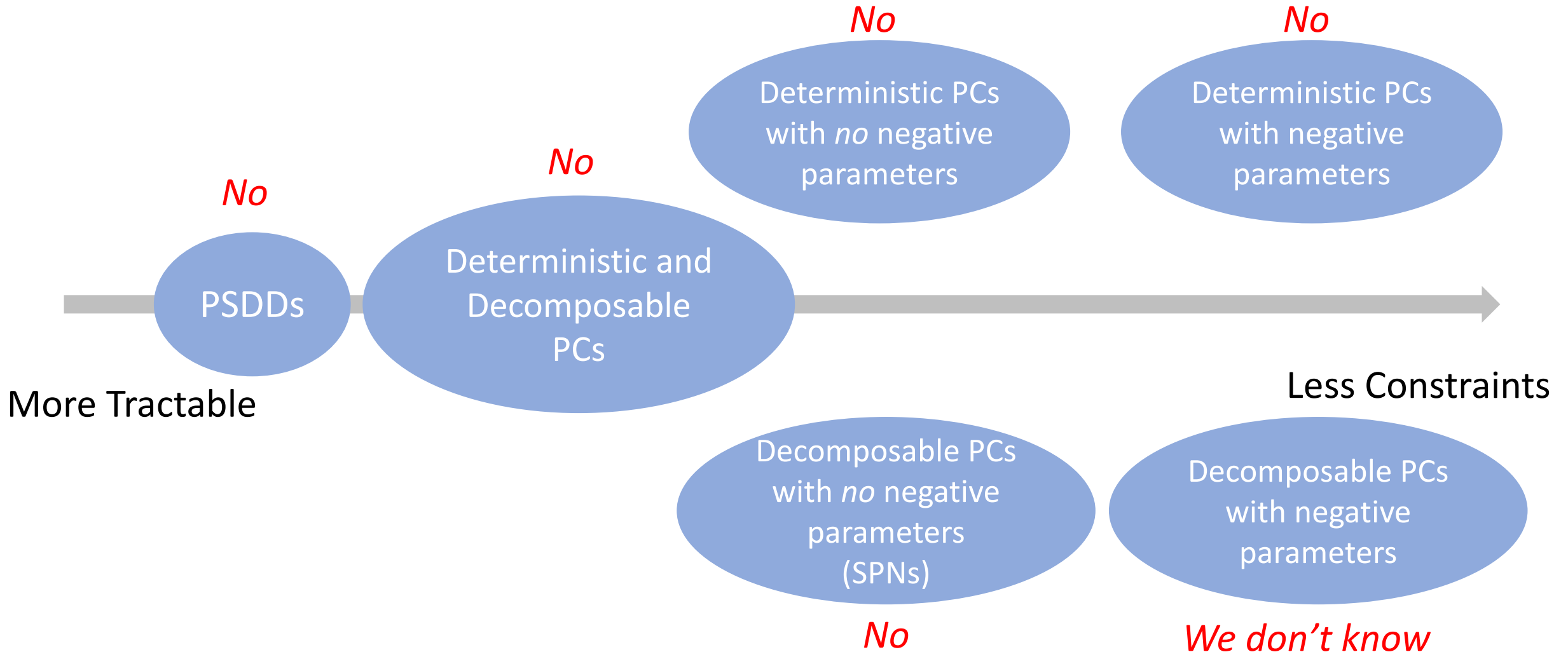
Fully
Factorized

Determinantal
Point Processes

?

?

We cannot tractably represent DPPs with subclasses of PCs



Negative Results

Theorem 1. *For a DPP with kernel $L = B^T B$, where B is randomly generated, **with probability 1**, this DPP cannot be represented by polynomial-size PSDDs.*

Theorem 2. *There exists a class of DPPs that cannot be tractably represented by deterministic PCs with (possibly) **negative parameters**.*

Theorem 3. *There exists a class of DPPs that cannot be tractably represented by PCs with **non-negative parameters** (SPNs).*